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COMPARISON OF 2-D AND 3-D EFFECTS ON VARIOUS GEOMETRY TO PREDICT THE EFFECTIVE THERMAL CONDUCTIVITY OF POROUS SYSTEM

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ABSTRACT

In this article, the 3-Dimensional numerical model has been developed for estimating effective thermal conductivity of porous system based on unit cell approach. The inherent 3-D problem is modeled using Finite Element Analysis for various inclusions (square, circular, hexagon and octagon). The model is tested with at different composition of solid to fluid fractions and solid to fluid conductivities. Comparison has been carried out for 2-Dimensional and 3-Dimensional effect for various inclusions for estimating the effective thermal conductivity of porous materials. The results shows that for higher concentration and conductivity ratio, the model with varying cross section estimates the effective thermal conductivity of two phase materials with higher accuracy.

KEYWORDS

Index Terms-2D-3D dimensional, Various inclusions, Conductivity ratio, Contact ratio, Porous systems and Concentration.

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INTRODUCTION

The theoretical estimation of the effective thermal conductivity (ETC) of two phase materials has been always difficult. Use of two-phase materials is regarded as more effective means of energy conservation and energy efficiency in an industrial sector. Numerous models were developed to find out the effective conductivity of mixtures, but one of the major limitations of the models is its suitability for specific application. Effective thermal conductivity of two phase material is very important to determine

heat transfer characteristics. Reddy and Karthikeyan¹ developed the collocated parameter model based on the unit cell approach for predicting the effective thermal conductivity of the two-phase materials. Tai² deduced mathematical expressions for the equivalent thermal conductivity of two and three-dimensional orthogonally fiber-reinforced composites in a one-dimensional heat flow model. In this regard, Tai applied the fundamental definitions of thermal conductivity and the simple rule of mixtures to a unit cell of an orthogonally fiber-reinforced material. Tai, showed that whether a square slab model or a cylindrical fiber model is used makes little difference to the heat flux; while the fiber volume fraction matters. Jones and Pascal³ developed a three-dimensional numerical finite-difference to calculate the thermal conductivity of a composite with two or more constituents to better understand how the relative quantities and distributions of the component materials, within a sample, affect the whole sample conductivity. Graham and McDowell⁴ estimated the transverse thermal conductivity of continuous reinforced composites containing a random fiber distribution with imperfect interfaces using finite-element analysis. Krach and Advani⁵ investigated the effect of void volume and shape on the effective conductivity of a unidirectional sample of a 3-phase composite using a numerical approach consisting of a unit cell. Their findings clearly showed that the influence of porosity on thermal conductivity could not be described solely by the void volume. They found that the shape and distribution of the voids influence the effective thermal conductivity. Al-Sulaiman *et al*⁶ developed correlations based on a finite element analysis that predict the thermal conductivity of fibers utilizing the easy to measure thermal conductivity of the Fiber Reinforced Composite Laminates (FRCL) and the other constituents. In their model, Al-Sulaiman *et al* considered the FRCL cured at high pressures such that it includes no air voids. Zou *et al*⁷. Come up with an analytical expression for transverse thermal conductivities of unidirectional fiber composites with and without thermal barrier is derived based on the electrical analogy technique and on the cylindrical filament-square packing array unit cell

model (C-S model). The effective thermal conductivity modeling of various inclusions has been carried out by A P Senthil Kumar⁸⁻⁹.

Symbols

- α Conductivity ratio(k_s/k_f)
- v Concentration
- λ Contact ratio(c/a)
- A Wall area (m^2)
- h Heat transfer coefficient ($W/m^2.K$)
- T_{conv} bulk temperature of the fluid at the convection side (K)
- T_{wall1} fixed wall temperature (K)
- T_{wall2} convective wall temperature (K).

NUMERICAL ANALYSIS FOR VARIOUS INCLUSIONS

Numerical heat transfer analysis of the unit cell for various inclusion shapes (square, hexagon, octagon and circular cylinders) has been carried out to estimate the ETC of porous materials via the Finite Element simulation. For this heat transfer analysis ANSYS, a finite element software package is used. Solid 90 element was used for the analysis and an element size of 0.03 was adopted. Software validation and mesh sensitivity test has been carried out

Boundary condition

One face of the unit cell is subjected to constant temperature and the opposite face is subjected to convective thermal environment. All other faces are kept as adiabatic in order to achieve 1D heat transfer. The boundary condition imposed on the unit cell is shown in the Figure No.1.

Determination of Effective Thermal conductivity

From the results of the finite element analysis, the average surface temperature on the convection wall of the unit cell is computed. Once the temperature of the convective side is known, the effective thermal conductivity across the two walls can be calculated using the following simple heat balance equation

$$hA(T_{wall2} - T_{conv}) = \frac{K_{eff} A(T_{wall1} - T_{wall2})}{L} \quad (1)$$

Mesh sensitivity test

Figure No.2. Shows the meshed model of the unit cell of the square cylinder. Three iterations have been carried out for the case of two-phase material

with conductivity ratio (α) = 800, concentration (v) = 0.5 and contact ratio (λ) = 0.02 for mesh-independent study. The finite element edge size was changed from very coarse to very fine, when performing the iterations. In each of these three runs, the average temperature at the convective wall of the two-phase material was obtained.

A summary of the results of iterations indicating the element edge size and the corresponding average wall temperature obtained for various inclusions is shown in Table No.1. It is observed that the average wall temperature remains almost constant after using an element edge size of 0.1, indicating the convergence of the solution. Hence, an element edge size of 0.1 is used for further analysis.

THREE - DIMENSIONAL MODELING FOR VARIOUS INCLUSIONS BASED ON PRIMARY AND SECONDARY PARAMETERS

A model with 3-Dimensional effect has been considered to estimate the ETC of porous materials. The unit cell of various inclusion shapes (square, circular, octagon and hexagon cylinder) has been modeled parametrically. The numerical modeling has been carried out for various inclusions by considering the primary and secondary parameters, viz., conductivity ratio, concentration and contact ratio. The inclusion shapes namely, square, hexagon, octagon having a side length of 'a' having a contact cube of side length 'c'. Similarly, circular cylinders having diameter 'a' and an inline contact plate of width 'c' and height 'δ'. The finite contact between the cylinders by connecting plates is denoted the contact parameter 'c/a'. Because of the symmetry of the plates, one fourth of the cross-section has been considered as a unit cell for all shapes of inclusions and is shown in Figure No.3 (a-d). For all inclusions, the first layer consists of solid phase with a dimension of $(c/2) (l/2)^2$. The second layer consists of solid and fluid phases dimensions of $((a-c)/2) (a/2)^2$ and $((a-c)/2) ((l-a)/2)^2$ for square cylinder. For third layer consists of solid and fluid phases dimensions of $((l-a)/2) (c/2)^2$ and $((l-a)/2) ((l-c)/2)^2$ for square cylinder. Similarly, for circular cylinder the second and third layer consists of solid and fluid phases dimensions of $((a-c)/2) (a/2)^2$ & $((a-c)/2) ((l-$

$a/2)^2$, and $(\delta/2) (c/2)^2$ and $(\delta/2) (l-c/2)^2$ respectively. For octagon cylinder the second and third layer consists of solid and fluid phases dimensions of $\{[a/2 + a/\sqrt{2}]-c/2\} (a/2 + a/\sqrt{2})^2$ and $\{[a/2 + a/\sqrt{2}]-c/2\} (l/2-(a/2+a/\sqrt{2}))^2$ and $(l/2-(a/2+a/\sqrt{2})) (c/2)^2$ and $(l/2-(a/2+a/\sqrt{2})) (l-c/2)^2$ respectively. Similarly, for hexagon cylinder the second and third layer consists of solid and fluid phases dimensions of $[a\sqrt{3}/2-c/\sqrt{2}] (a/2+\{a/\sqrt{2}-c/2\sqrt{3}\})^2$ & $[a\sqrt{3}/2-c/\sqrt{2}] (l/2-(a/2+\{a/\sqrt{2}-c/2\sqrt{3}\}))^2$ and $(l/2-(a\sqrt{3}/2)) (c/2)^2$ and $(l/2-(a\sqrt{3}/2)) (l-c/2)^2$ respectively.

COMPARISON RESULTS OF 2-DIMENSIONAL AND 3-DIMENSIONAL EFFECTS ON NUMERICAL MODELING FOR VARIOUS INCLUSIONS WITH EXPERIMENTAL DATA

The numerically predicted effective thermal conductivity values for square, hexagon, octagon and circular cylinders models have been compared with published experimental data for porous granular materials and found that 3-dimensional numerical values predicted are quite close to the experimental results with high accuracy. A comparison of 2-dimensional and 3-dimensional numerical models with experimental data for different concentrations and conductivity ratios has been made for porous materials and is given in the Table No.1 (a-b). Experimental data for various two-phase systems were taken from reported studies. For porous granular materials [$v = 0.2$ to 0.740 and $\alpha = 7.368$ to 233.653], the 3-Dimensional circular cylinder model having very close agreement with the experimental data compared with other geometry's. The range of accuracy appears quite good in consideration with the variety of sources of data selected and the wide range of shapes included. It is observed that the 3-Dimensional circular cylinder model has an average deviation of ± 1.89 % from experimental data as against ± 6.67 % of square cylinder, ± 4.97 % of hexagon cylinder and ± 3.07 % of octagon cylinder respectively with 3-Dimensional effect Table No.2 (a-b). For the same range, 2-Dimensional numerical model having the minimum and maximum deviation of ± 43.53 % and ± 57.95 % respectively for various inclusions is shown in Table No.1 (a-b). It is clearly indicate that the 3-Dimensional numerical model is

Table No.2: b. Comparison on two dimensional and three dimensional effects on numerical effective thermal conductivity with experimental data for porous system

S.No	k_s	k_f	α (k_s/k_f)	ν	k_{exp}	λ (c/a) OCT	k_{octa}				λ (c/a) HEX	k_{hex}			
							3D	Devi	2D	Devi		3D	Devi	2D	Devi
1	1.099	0.024	45.792	0.74	0.227	0.7	0.227	0.007	0.541	58.04	0.85	0.2202	3.096	0.658	65.5
2	1.099	0.024	45.792	0.2	0.041	0.05	0.0403	1.851	0.051	19.61	0.05	0.0428	4.166	0.0584	29.79
3	12.414	0.586	21.184	0.569	2.544	0.81	2.5478	0.149	5.052	49.64	0.8	2.4224	5.018	5.2434	51.48
4	20.864	0.337	61.911	0.495	2.009	0.33	2.0036	0.267	4.718	57.42	0.27	2.049	1.955	4.927	59.22
5	1.061	0.144	7.368	0.57	0.406	0.33	0.3448	17.76	0.464	12.5	0.01	0.341	19.05	0.3812	6.506
6	34.347	0.147	233.65	0.62	2.14	0.22	2.1594	0.899	3.649	41.35	0.16	2.1634	1.084	5.755	62.81
7	34.347	0.179	191.88	0.62	2.429	0.25	2.428	0.042	3.897	37.67	0.18	2.409	0.832	5.231	53.57
8	34.347	0.627	54.78	0.62	5.404	0.69	5.3993	0.088	8.039	32.78	0.6	5.3867	0.322	14.618	63.03
9	2.001	0.021	95.286	0.47	0.12	0.17	0.1217	1.379	0.295	59.32	0.1	0.1105	8.592	0.257	53.31
10	33.764	0.586	57.618	0.6	4.329	0.45	4.3105	0.429	4.863	10.98	0.37	4.3178	0.26	6.398	32.34
11	2.001	0.03	66.7	0.58	0.23	0.41	0.2308	0.348	0.615	62.6	0.32	0.2311	0.478	0.628	63.38
12	2.001	0.03	66.7	0.64	0.281	0.55	0.2791	0.683	0.788	64.34	0.45	0.2793	0.622	0.816	65.56
13	2.001	0.03	66.7	0.7	0.364	0.9	0.3645	0.131	1.042	65.07	0.75	0.3533	3.037	1.07	65.98
14	1.201	0.028	42.893	0.65	0.22	0.79	0.2205	0.212	0.554	60.29	0.75	0.2209	0.412	0.586	62.46
15	1.201	0.14	8.579	0.65	0.5	0.05	0.4333	15.39	0.522	4.215	0.01	0.4275	16.96	0.471	6.157
16	5.003	0.62	8.069	0.676	2.331	0.05	2.0043	16.3	2.248	3.692	0.1	1.9254	21.06	2.399	2.835
17	1.091	0.029	37.621	0.6	0.18	0.63	0.1814	0.794	0.619	70.92	0.6	0.1848	2.612	0.46	60.87
18	1.046	0.026	40.231	0.65	0.193	0.75	0.1923	0.346	0.478	59.62	0.7	0.1909	1.086	0.506	61.86
19	1.046	0.133	7.865	0.639	0.452	0.04	0.3859	17.13	0.432	4.63	0.01	0.3813	18.53	0.42	7.619
20	8.374	0.129	64.915	0.485	0.722	0.27	0.7201	0.259	1.683	57.1	0.2	0.7132	1.228	1.682	57.07
21	8.374	0.147	56.966	0.64	1.323	0.65	1.3015	1.654	3.497	62.17	0.6	1.3312	0.62	3.7344	64.57
22	8.374	0.147	56.966	0.41	0.598	0.2	0.5978	0.032	0.656	8.841	0.15	0.5974	0.107	1.219	50.94
23	2.932	0.023	127.48	0.456	0.169	0.19	0.1684	0.333	0.426	60.33	0.15	0.175	3.425	0.438	61.42
24	2.932	0.023	127.48	0.552	0.221	0.26	0.2207	0.139	0.65	66	0.2	0.2256	2.034	0.663	66.67
25	1.13	0.026	43.462	0.6	0.176	0.6	0.1766	0.365	0.431	59.16	0.4	0.1633	7.767	0.418	57.89
Average deviation								3.079		43.53			4.974		49.31

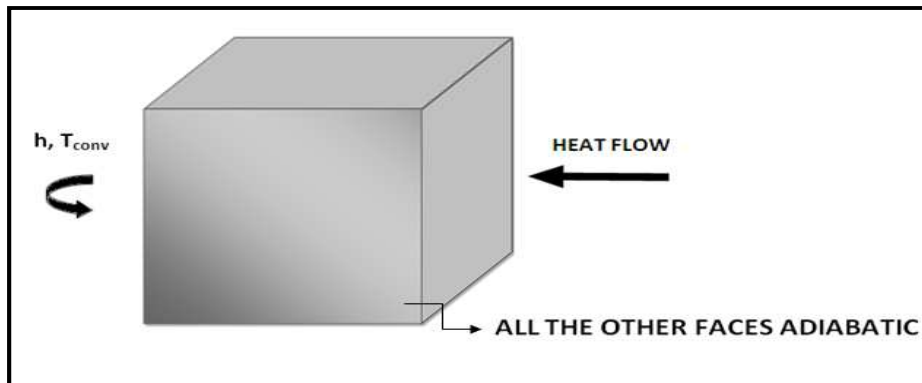


Figure No.1: The Thermal boundary condition applied on the unit cell

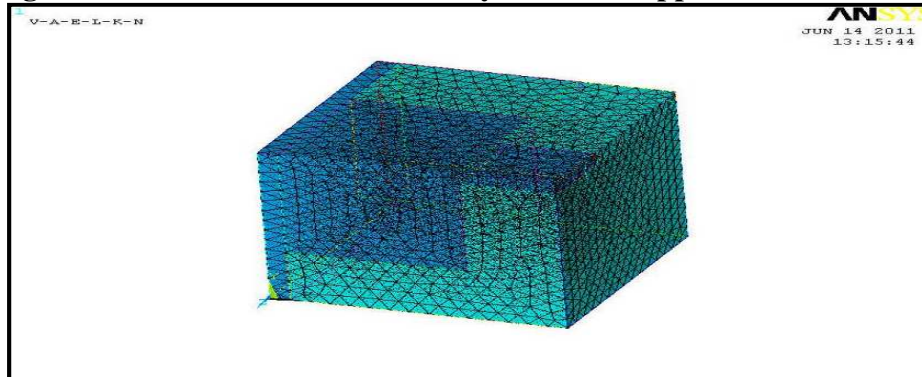
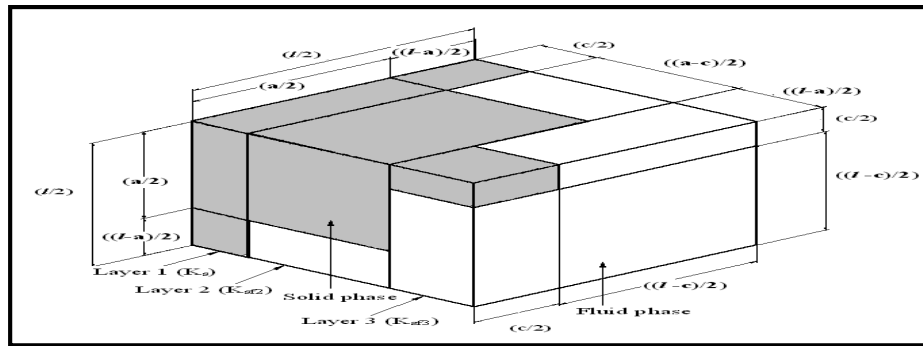
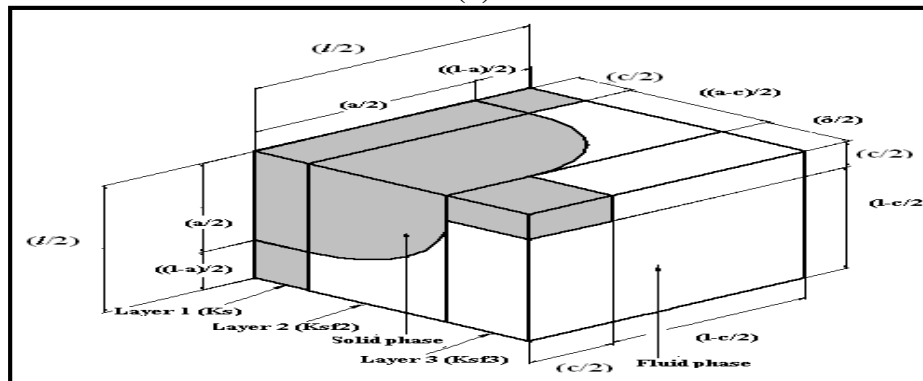


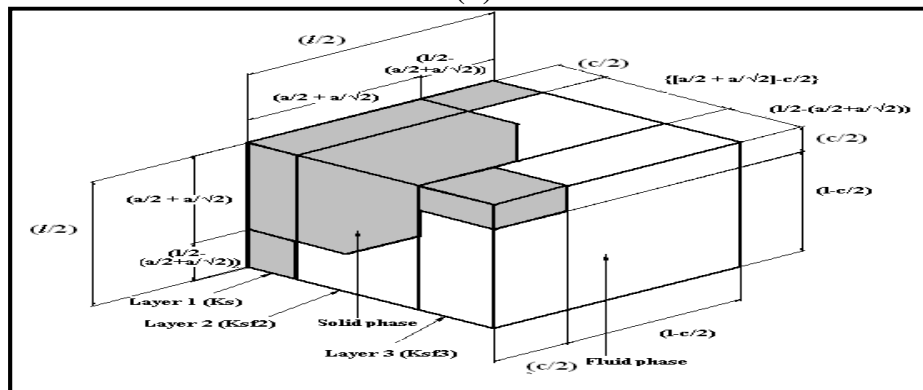
Figure No.2: Meshed model of unit cell for square cylinder



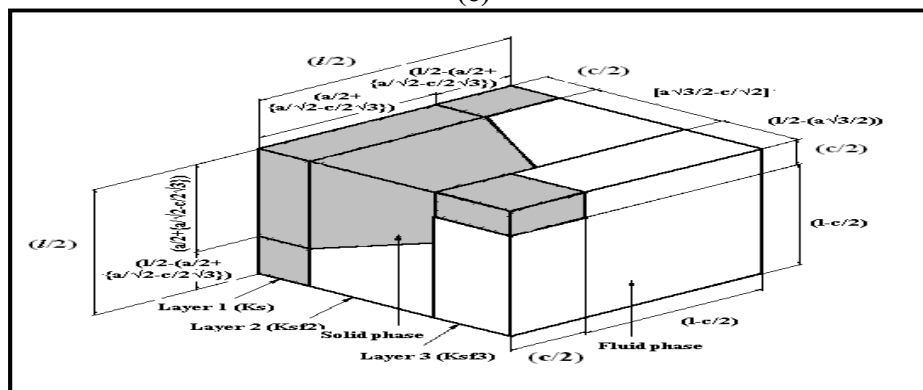
(a)



(b)



(c)



(d)

Figure No.3: Two dimensional periodic two-phase system: (a) Square cylinder (b) Circular cylinder (c) Octagon cylinder (d) Hexagon cylinder

CONCLUSION

The comparison has been made between the constant and varying cross sections with available experimental data. It clearly indicates that model with varying cross section predicts the effective thermal conductivity better than the model with constant cross section.

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CONFLICT OF INTEREST

We declare that we have no conflict of interest.

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